TEMPERATURE BEHAVIOUR OF OPTICAL ABSORPTION EDGE AND PHASE TRANSITIONS IN Cu₆PS₅I_{0.8}Cl_{0.2} SUPERIONIC MIXED CRYSTALS

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Isoabsorption and spectral temperature studies of absorption edge of $Cu_6PS_5I_{0.8}Cl_{0.2}$ superionic mixed crystals are performed. Phase transition temperatures are determined and the transitions are identified. The optical absorption edge shape is studied in the temperature range 77–320 K, the parameters of electron-phonon interaction, resulting in the Urbach behaviour of the optical absorption edge, are determined, temperature dependences of the optical pseudogap and Urbach energy are obtained.

Keywords: superionic mixed crystals, optical absorption edge, Urbach rule, phase transitions

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1. Introduction

 Cu_6PS_5X (X = I, Cl) superionic conductors belong to the compound with argyrodite crystal structure and are characterized by high values of electrical conductivity and low values of activation energy [1-3]. At low temperatures these crystals undergo two phase transitions, one of them being a first-order superionic phase transition which is realised at $T_{\rm I} = 170$ K for Cu₆PS₅I and $T_{\rm I} = 165$ K for Cu₆PS₅Cl, and the other is a secondorder structural phase transition which is realised at $T_{\rm II} = 269$ K for Cu₆PS₅I and $T_{\rm II} = 241$ K for Cu₆PS₅Cl [4, 5]. At room temperature $(T > T_{II})$ Cu₆PS₅X crystals belong to the cubic syngony ($F\bar{4}3m$ space group) [1]. According to Ref. [6], at $T_{\rm I} < T < T_{\rm II} \, {\rm Cu}_6 {\rm PS}_5 {\rm I}$ crystals belong to a cubic superstructure ($F\bar{4}3c$ space group), while at $T < T_{I}$ to the monoclinic syngony (*Cc* space group).

Thermodynamical, dielectric, acoustic, and optical properties of Cu_6PS_5X crystals were studied in Refs. [4, 5, 7–12]. It should be noted that the earlier studies of Cu_6PS_5I crystal absorption edge at high absorption levels have shown the existence of bound and free excitons at temperatures below the superionic phase transition, which undergo considerable changes with the temperature increase [11]. At the transition to the superionic state not only the exciton structure is changed, but also exponential parts at the longwave absorption edge appear. Contrary to Cu₆PS₅I, in Cu₆PS₅Cl crystal [12] no excitonic bands are observed near the absorption edge at low temperatures. At $T > T_1$ for Cu₆PS₅X crystals the temperature behaviour of exponential parts of the absorption edge is described by the empirical Urbach rule [13]:

$$\alpha(h\nu, T) = \alpha_0 \exp\left[\frac{\sigma(h\nu - E_0)}{kT}\right] = \alpha_0 \exp\left[\frac{h\nu - E_0}{E_{\rm U}(T)}\right],\tag{1}$$

where $E_{\rm U}$ is the Urbach energy (a reciprocal of the absorption edge slope $E_{\rm U}^{-1} = \Delta(\ln \alpha)/\Delta(h\nu)$), σ is the absorption edge steepness parameter, α_0 and E_0 are the convergence point coordinates of the Urbach bundle.

The present work is aimed at the crystal growth, isoabsorption, and spectral studies of optical absorption edge as well as influence of I \rightarrow Cl anionic substitution and related compositional disordering of the crystal lattice on the phase transitions and optical absorption edge parameters in Cu₆PS₅I_{0.8}Cl_{0.2} superionic mixed crystals.

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2. Experiment

Cu₆PS₅I_{0.8}Cl_{0.2} mixed crystals were grown using chemical vapour transport method. The synthesis from extra pure Cu, P, S, and CuX (X = I, Cl) compounds, additionally purified by distillation in vacuum, was performed. 10–20 mg of CuI and CuCl in corresponding proportion per 1 cm³ of the ampoule free volume were used as a transport agent. The temperature at the hot end of the vessel was kept at 923 to 973 K, and at the cool one at 873 to 923 K. Thus grown crystals had the shape of plane-parallel plates (5×5×2 mm³) or distorted tetrahedrons (4×4×4 mm³).

The isoabsorption temperature studies consisted in measuring the absorption edge energy position E_g^{α} at the fixed value of absorption coefficient α . Spectral dependence of the absorption coefficient α was studied in the temperature range 77–320 K using the set-up described in Ref. [14]. A MDR-3 diffraction monochromator was used for transmittance and reflectance measurements. The spectral slit was about 1 Å. A UTREX cryostat was applied, the temperature being stabilized within 0.1 K. The linear absorption coefficient α as a function of transmittance Tr and reflection of the surface R were calculated using the well-known formula,

which takes into account multiple internal reflections [14]:

$$\alpha = \frac{1}{d} \left\{ \frac{(1-R)^2}{2Tr} + \sqrt{\left[\frac{(1-R)^2}{2Tr}\right]^2 + R^2} \right\}, \quad (2)$$

where d denotes the plane-parallel sample thickness. The sample thicknesses in our measurements varied from 50 to 100 μ m, the relative error in the absorbance measurements $\Delta \alpha / \alpha$ not exceeding 10% at $0.3 \le \alpha d \le$ 3 [15].

3. Results and discussion

The isoabsorption studies showed that within the temperature interval 77–130 K the spectral position of absorption edge E_g^{α} remains unchanged, at T > 130 K the absorption edge shifts to the long-wavelength side, at $T_{\rm I} = (184\pm1)$ K (determined at heating) the anomalous stepwise behaviour of the E_g^{α} with $dE_g^{\alpha}/dT > 0$ is observed (Fig. 1). The stepwise behaviour of E_g^{α} and temperature hysteresis $\Delta T = 6$ K describe the phase transition at $T = T_{\rm I}$ as the first-order phase transition. The long-wavelength shift of absorption edge is observed at $T > T_{\rm I}$ and typical change of the slope of the $E_g^{\alpha}(T)$ plot is realized in the temperature interval of the second-order phase transition $T_{\rm II} = (240-260)$ K.

Absorption edge studies in $Cu_6PS_5I_{0.8}Cl_{0.2}$ crystals have shown that in the temperature interval un-



Fig. 1. Temperature dependences of the optical pseudogap E_g^* (1) and absorption edge energy position E_g^{α} at $\alpha = 250 \text{ cm}^{-1}$ (2) at cooling and heating in Cu₆PS₅Cl_{0.2}I_{0.8} mixed crystals. The solid lines are drawn to guide the eye, the dashed line is obtained by fitting the data for $T > T_{\text{II}}$ to the Eq. (4).

der investigation the absorption edge has exponential shape, at $T > T_{\rm I}$ the temperature behaviour of absorption edge is described by the Urbach rule, the coordinates of the Urbach absorption edge convergency point remain unchanged at $T = T_{\rm II}$ and have the values $\alpha_0 = 4.04 \cdot 10^5$ cm⁻¹ and $E_0 = 2.229$ eV (Figs. 2, 3). From the temperature dependence of the absorption edge steepness parameter σ , the parameters of electron–phonon interaction (EPI) are obtained according to [16]:

$$\sigma(T) = \sigma_0 \frac{2kT}{\hbar\omega_{\rm p}} \cdot \tanh\left(\frac{\hbar\omega_{\rm p}}{2kT}\right),\tag{3}$$

where $\hbar \omega_p$ is the effective phonon energy in a singleoscillator model, describing the EPI, and σ_0 is a param-



Fig. 2. Spectral dependences of Cu₆PS₅Cl_{0.2}I_{0.8} mixed crystal absorption coefficient at various temperatures: *1* at 83 K, 2 at 140 K, 3 at 160 K, 4 at 180 K, 5 at 200 K, 6 at 220 K, 7 at 240 K, 8 at 260 K, 9 at 280 K, *10* at 300 K.



Fig. 3. Spectral dependences of the Urbach absorption edge for Cu₆PS₅Cl_{0.2}I_{0.8} mixed crystals at various temperatures: 1 at 200 K, 2 at 220 K, 3 at 240 K, 4 at 260 K, 5 at 280 K, 6 at 300 K. The inset shows the temperature dependence of steepness parameter σ.

Table 1. Convergence point coordinates α_0 and E_0 of the Urbach absorption edge, parameters of EPI $\hbar\omega_p$ and σ_0 , Einstein temperature Θ_E , phase transition temperatures T_I and T_{II} , parameters $E_g^*(0)$, S_g^* , $(E_U)_0$, and $(E_U)_1$ for Cu₆PS₅I and Cu₆PS₅Cl single crystals as well as for Cu₆PS₅I_{0.8}Cl_{0.2} mixed crystals.

Crystal	Cu ₆ PS ₅ I		$Cu_6PS_5Cl_{0.2}I_{0.8}$		Cu ₆ PS ₅ Cl	
Temperature region	$T > T_{\mathrm{II}}$	$T < T_{\mathrm{II}}$	$T > T_{\rm II}$	$T < T_{\mathrm{II}}$	$T > T_{\mathrm{II}}$	$T < T_{\mathrm{II}}$
$\alpha_0, \mathrm{cm}^{-1}$	$2.96 \cdot 10^{6}$		$4.04 \cdot 10^5$		$4.26 \cdot 10^4$	
E_0, eV	2.230		2.229		2.776	
σ_0	1.55	1.52	1.34	1.51	0.27	0.28
$\hbar\omega_{\rm p}, {\rm meV}$	32	27	22	36	57	58
Θ_E, \mathbf{K}	371	313	252	416	662	673
$(E_{\rm U})_0$, meV	9.6	9.9	8.2	11.8	105.5	104.8
$(E_{\rm U})_1$, meV	23.2	15.8	16.2	23.8	191.8	200.0
$E_g^*(0)$, eV	2.152	2.157	2.173	2.170	2.384	2.392
S_g^*	5.6	5.4	6.1	5.9	12.0	14.5
$T_{\rm I},{ m K}$	170		184		165	
$T_{\mathrm{II}}, \mathbf{K}$	269		240-260		241	

eter related to the EPI constant g via $\sigma_0 = (2/3)g^{-1}$. The values of the effective phonon energy $\hbar\omega_p$ and the EPI parameter σ_0 , obtained at the description of $\sigma(T)$ dependence (see the insets to Fig. 3), are listed in Table 1. For comparison the Urbach edge parameters and EPI parameters as well as the phase transition temperatures for Cu₆PS₅I and Cu₆PS₅Cl single crystals are also listed in Table 1. In Cu₆PS₅I_{0.8}Cl_{0.2} mixed crystals $\sigma_0 > 1$, this being the evidence for weak EPI [17]. It should be noted that in the range of the phase transitions the features in the temperature dependence of σ are observed (see the insets to Fig. 3) as well as the variation of $\hbar\omega_p$ and σ_0 parameter values at $T = T_{\rm II}$ (Table 1).

Temperature dependences of the Urbach absorption edge parameters – optical pseudogap E_g^* (E_g^* is the absorption edge energy position at the fixed value of the absorption coefficient $\alpha = 1000 \text{ cm}^{-1}$ [12]) and Urbach energy E_U are shown in Fig. 4. The temperature dependences of E_g^* and E_U for the temperature range where the Urbach shape of absorption edge is observed are well described in the framework of Einstein model by the relationships [18, 19]

$$E_{g}^{*}(T) = E_{g}^{*}(0) - S_{g}^{*} k \Theta_{\mathrm{E}} \left[\exp\left(\frac{\Theta_{\mathrm{E}}}{T}\right) - 1 \right]^{-1},$$
(4)

$$E_{\rm U} = (E_{\rm U})_0 + (E_{\rm U})_1 \left[\exp\left(\frac{\Theta_{\rm E}}{T}\right) - 1 \right]^{-1},$$
 (5)

where S_g^* is a dimensionless constant of interaction, Θ_E is the Einstein temperature corresponding to the average frequency of phonon excitations of a system of noninteracting oscillators, $(E_U)_0$ and $(E_U)_1$ are constant values. The Einstein temperature is related to the Debye temperature Θ_D as $\Theta_E \approx (3/4)\Theta_D$ [20]. The adjustment parameters $E_g^*(0)$, S_g^* , Θ_E , $(E_U)_0$, and $(E_U)_1$ are listed in Table 1. The most noticeable anomaly in the range of the phase transitions is observed at $T = T_I$ in the temperature dependence of E_U (Fig. 4). Other features are revealed weakly that can be related to the Cu₆PS₅I_{0.8}Cl_{0.2} mixed crystal lattice disordering.

The Urbach energy is known to characterize the degree of edge smearing due to the crystal lattice disordering caused by specific features of its structure as well as induced by external factors [21]. Besides the temperature-related disordering due to thermal vibrations of the lattice, superionic crystals are characterized by structural disordering. In superionic conductors the structural disordering is caused by non-equivalence between the number of mobile ions and positions which they can occupy, and is related only to the sublattice of the mobile ions since the rigid sublattice preserves its regular structure. In Ref. [12] it was shown for Cu₆PS₅X crystals that in fast-ion conductors the structural disordering in superionic phase consists of two components - dynamical and static. Static structural disordering in Cu₆PS₅X crystals, due to the structure deficiency, results in local non-uniform electric fields which, in turn, result in additional smearing of the band edges. Dynamical structural disordering in the superionic phase arises due to the hopping motion of copper ions participating in ion transport and providing high ionic conductivity.

In $Cu_6PS_5I_{0.8}Cl_{0.2}$ mixed crystals, besides the temperature-related (due to the lattice thermal vibrations) and structural (static and dynamical) disordering typical of pure Cu_6PS_5X crystals, compositional disordering should also be revealed. According to Ref. [22], the



Fig. 4. Temperature dependences of the optical pseudogap E_g^* (1) and Urbach energy E_U (2) for Cu₆PS₅Cl_{0.2}I_{0.8} mixed crystals. The lines are drawn to guide the eye.

effect of different types of disordering on the Urbach energy in mixed crystals is given by

$$E_{\rm U} = (E_{\rm U})_{\rm X} + (E_{\rm U})_T + (E_{\rm U})_{\rm C} = (E_{\rm U})_{\rm X,C} + (E_{\rm U})_T,$$
(6)

where $(E_U)_X$ and $(E_U)_C$ are the contributions of static structural and compositional disordering, respectively, and $(E_U)_T$ reflects the effect of temperature-dependent types of disordering. It follows from the comparison of Eqs. (5) and (6) that $(E_U)_{X,C} \equiv (E_U)_0$ and $(E_U)_T \equiv$ $(E_U)_1/[\exp(\Theta_E/T) - 1]$. This enables one to estimate the contribution of various types of disordering into the Urbach energy E_U . The performed calculations have shown that the contribution of $(E_U)_{X,C}$ into E_U at T =300 K is 40% while that of $(E_U)_T$ is 60%. Thus, the absorption edge smearing at T = 300 K results mostly from the effect of temperature-dependent types of disordering, i. e. the effect of thermal vibrations of the lattice and dynamical structural disordering in the superionic phase due to the hopping motion of copper ions.

4. Conclusions

Absorption edge studies in Cu₆PS₅I_{0.8}Cl_{0.2} mixed crystals have shown that in the temperature interval under investigation the absorption edge has exponential shape, at $T > T_{\rm I}$ the temperature behaviour of absorption edge is described by the Urbach rule, the coordinates of the Urbach absorption edge convergency point remain unchanged at $T = T_{\rm II}$. From the temperature dependence of the absorption edge steepness parameter σ , the parameters of electron–phonon interaction are obtained. The temperature dependences of Urbach absorption edge parameters such as optical pseudogap E_g^* and Urbach energy E_U are well described in the framework of Einstein model. The analysis of Urbach absorption edge has shown a change of the character of the temperature dependences of σ , E_U , and E_g^* to be observed at the phase transitions.

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OPTINIO SUGERTIES KRAŠTO TEMPERATŪRINIS ELGESYS IR FAZINIAI VIRSMAI Cu₆PS₅I_{0.8}Cl_{0.2} SUPERJONINIAME LAIDININKE

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Santrauka

Atlikti maišyto $Cu_6PS_5I_{0,8}Cl_{0,2}$ kristalo izosugerties ir sugerties krašto spektriniai bei temperatūriniai tyrimai, identifikuoti faziniai virsmai ir įvertintos jų temperatūros. Optinės sugerties krašto forma buvo tiriama 77–300 K temperatūroje, nustatyti optinės sugerties krašto Urbacho elgesį lemiančios elektrono ir fonono sąveikos parametrai bei optinio pseudotarpo ir Urbacho energijos temperatūrinės priklausomybės.