

DEPOPULATION MECHANISM FOR INCOHERENT TERAHERTZ SOURCE – THz TORCH – BASED ON GaAsBi/GaAs QUANTUM WELL IN GaAs/AlGaAs PARABOLIC QUANTUM WELL

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Parabolic quantum wells (PQWs) are known as a promising candidate for a compact terahertz (THz) source. PQWs have equidistant subbands that can be designed to be separated by few meV to meet the THz frequency range. To enhance the efficiency and power of THz emission from PQWs, a new approach is proposed by employing depopulation of the lowest subbands of PQW. In this work, the theoretical analysis of an incoherent THz torch device is presented. The findings suggest that the introduction of narrower band-gap GaAsBi/GaAs rectangular quantum well within the GaAs/AlGaAs PQW can alter subbands arrangement to enable a faster depopulation mechanism exploiting LO phonon scattering. The calculated radiative power spectra show the increase of oscillator strength between the rearranged subbands of PQW due to the added GaAsBi rectangular potential. The increased intersubband radiative transition probability can lead to an efficient compact incoherent THz source – THz torch.

Keywords: terahertz emission, parabolic quantum well, GaAsBi/GaAs/AlGaAs nanostructures, incoherent THz source

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1. Introduction

Terahertz (THz) frequency waves are situated in the electromagnetic spectral range between microwave and far-infrared radiation from 0.1 to 10 THz. THz waves exhibit unique physical properties that can be used for many applications in spectroscopy, for instance, food inspection [1, 2], materials characterization [3] or medical diagnosis [4, 5]. THz imaging has opened new routes for application in discrimination of hidden or packaged objects [6, 7], medical characterization [8, 9] or near-field sub-wavelength microscopy [10, 11]. It can be possible because of the fact that many opaque to visible light materials, such as paper, plastic and cloth, are transparent to THz frequency waves, albeit many chemical compounds have unique signature THz spectrum absorption lines that identify the composition of the sealed content. The advan-

tage is the non-ionizing and non-destructive nature of THz spectroscopy and imaging techniques that do not affect the samples under the test due to the small energy of THz radiation ranging from 0.4 to 41 meV in terms of photon energy. Yet another emerging application field is sub-THz and THz range communication for high-speed, -volume data transmission due to the wide spectral band of radiation [12].

To fully enable advantages of THz spectroscopy and imaging as compared to other competing techniques, such as infrared spectroscopy and X-ray imaging, and to expand the application field, compact and low-cost systems are required. For this purpose, a lot of efforts are dedicated to develop a new type of detectors [13, 14] and passive radiation beam manipulation elements, such as lenses, mirrors and beam-splitters [15–17]. In fact, the recent development of micro-detectors allowed

one to achieve record values of sensitivity and noise equivalent power, in particular, employing heterodyning [18, 19] or homodyning [20] detection schemes. While the progress in the field of THz sensors has been impressive, the progress in the field of compact sources has been rather modest [21, 22].

Parabolic quantum wells (PQWs) are known as a promising candidate for a compact THz source. PQW has equidistant quantum energy subbands that can be designed to be separated by few meV to meet the THz frequency range [23]. Moreover, PQWs are little sensitive to thermal influence [24, 25] and applied electric fields [25, 26]. Therefore, the THz emission from PQWs was observed even at temperatures $Tk_b > \Delta E$, where k_b is the Boltzmann constant and ΔE is the energy difference between two adjacent subbands in the PQW [24].

Ulrich et al. reported the experimental value of electrically driven THz range PQW emitter efficiency to be 4.4×10^{-8} [24]. In that work, the metal grading was used to extract the intersubband radiation from the PQW. In fact, better performance in the sense of efficiency was measured for the 140 nm width over the 200 nm PQW design that corresponds to the measured intersubband radiation emission at 2.2 over 1.6 THz, respectively. The emission was observed up to 240 K temperature and the increase of non-radiative lifetime was responsible for thermal quenching. In another work by Bratschitsch et al., coherent THz emission was measured from optically pumped intersubband plasmons in doped PQW, and apparently the field screening was responsible for the THz emission from the PQWs and not the quantum beats [25]. In that work, the 140-nm-wide PQW yielded the intersubband emission at 2.55 THz. The spectral emission line was observed up to 150 K. The measured broadening of the line with increasing temperature suggested that increasing optical phonon scattering diminishes the THz intersubband radiation. Several other experimental works implement PQWs for advanced polaritonic THz emitters employing the strong light-matter coupling regime [27–30]. It is worth noting that all aforementioned studies employed the digital alloying technique for the growth of GaAs/AlGaAs PQWs.

Recently we have demonstrated the technological viability to grow the PQW GaAs/AlGaAs nanostructures using the analog alloying technique

with molecular beam epitaxy and insertion of the GaAsBi rectangular quantum well (QW) at the centre of PQW with a high amount of Bi up to 6% [31]. Parabolically graded nanostructures showed superior interband radiative properties over the step-like and conventional rectangular QWs containing Bi. The enhancement in photoluminescence was attributed to the increased carrier trapping efficiency and pronounced localization effect on the GaAsBi QW created by PQW. In another recent work, we have reported the investigation results of undoped GaAs/AlGaAs PQW with a central GaAsBi QW optical response in the THz spectral range [32]. The study revealed the spectral features at 4.69 and 7.1 THz that were tentatively attributed to the intersubband transitions of light holes in the valance band and electrons in the conduction band in GaAs/AlGaAs PQW grown using the analog alloying technique.

In this work, a new approach for an incoherent THz emitter based on GaAs/AlGaAs PQWs with carrier depopulation of the lowest subbands is proposed and theoretically analysed. Two designs for 2.5 and 7 THz frequency emitters are modelled using the one-dimensional stationary Schrödinger equation solver for semiconductor heterostructures. The electron intersubband radiative lifetime is calculated for PQWs and quantum efficiency is estimated in respect to other electron scattering processes. The rectangular GaAsBi/GaAs QW is added to the centre of PQW to enable the carrier depopulation mechanism with a faster electron scattering with LO phonons. The quantum structures are modelled with the best arrangement of subbands and quantum efficiency is compared for electron intersubband radiative lifetime between the two lowest subbands with and without LO phonon scattering. Radiative power spectra of the 2.5 and 7 THz frequency emitter designs are calculated to evaluate the impact of additional GaAsBi/GaAs QW potential at the bottom of GaAs/AlGaAs PQW on radiative properties. Finally, the THz torch device based on GaAs/AlGaAs PQWs with a faster depopulation of the lowest PQW subbands is proposed.

2. Modelling of PQWs for THz torch

GaAs/Al_xGa_{1-x}As PQWs with equidistant energy levels separated by 10.34 and 28.95 meV to meet

the frequency of 2.5 and 7 THz, respectively, are designed. The Al content x in the outer barriers is set to 30% in the AlGaAs alloy. The room temperature band gap energy 1.426 eV was taken for GaAs [33, 34] and, for AlGaAs barriers, the band gap was estimated using the linear dependence $E_g(x) = (1.426 + 1.247x)$ eV [35]. Then the room temperature $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ band gap energy is equal to 1.8 eV. The barrier potential height V_b for electrons is calculated accounting for 67% of total discontinuity in the conduction band and the rest in the valence band [36]. Then the barrier height for the conduction band V_b is 250.6 meV. The parabolic potential energy V as a function on the distance in z axis can be written as

$$V(z) = V_b \left[\left(\frac{2(z - z_0)}{l_w} \right)^2 + c_q \left(\frac{2(z - z_0)}{l_w} \right)^4 \right], \quad (1)$$

where z_0 is the coordinate of the PQW centre, l_w is the well width, and c_q is the empirical parameter to the weight quartic term set to 0.13. The addition of quartic to square term compensates the effect of electron effective mass increase and improves the equidistant arrangement of subbands [37] as it is going to be elucidated later. For the electron effective mass m^* , the Al content dependent linear growth relation $m^* = (0.067 + 0.083x)m_0$ was adopted [34, 38]. In terms of potential energy $V(z)$, this linear effective mass growth was redefined as $m^* = (0.067 + c_m V(z))m_0$ with the coefficient c_m equal to 0.09936 eV^{-1} .

In addition to the PQW modelled using Eq. (1), a rectangular GaAsBi/GaAs QW formed by introducing bismuth to GaAs was created in the centre of PQW. In the case of bismuth, a strong band gap shrinking effect was taken into account by the coefficient 65 meV per 1% of the Bi content y and assuming 45% of narrowing to be associated with the conduction band [39]. In the $\text{GaAs}_{1-y}\text{Bi}_y$ region, the effective mass value $0.0592m_0$ was set considering the experimental data [31, 40]. Thus, Eq. (1) for the PQW potential energy for the $\text{Al}_x\text{Ga}_{1-x}\text{As}$ region is supplemented with $V(z) = 0.45yV_{bb}$ for $|z| \leq l_c/2$ only and with limitation $V \leq V_0$, where z is the coordinate accounted from the $\text{GaAs}_{1-y}\text{Bi}_y$ QW centre, l_c is the width of central rectangular $\text{GaAs}_{1-y}\text{Bi}_y$ potential, and $V_{bb} = 6.5 \text{ eV}$ is the potential height value for GaBi.

With the above defined band parameters the one-dimensional stationary Schrödinger equation for semiconductor heterostructures with variable effective mass is solved,

$$-\frac{\hbar^2}{2} \frac{\partial}{\partial z} \frac{1}{m^*(z)} \frac{\partial \psi(z)}{\partial z} + V(z)\psi(z) = E\psi(z), \quad (2)$$

using a numerical solver based on preliminary estimations of the shooting method combined with the accurate and fast-converging energy E and the wavefunction $\psi(z)$ coupled solution method which in turn relays on the Newton convergence scheme and internal bordered tridiagonal matrix solver [41]. The transitions between initial ψ_i and final states ψ_f were characterized with the dipole matrix element [37]

$$d_{if} = \langle \psi_i | z | \psi_f \rangle. \quad (3)$$

The oscillator strength S_{if} is proportional to the square of d_{if}

$$S_{if} = \frac{2m^*}{\hbar^2} \hbar v_{if} d_{if}^2, \quad (4)$$

where $\hbar v_{if} \equiv \Delta E$ is the energy difference between two subbands. Knowing the oscillator strength for transitions among every subband in the system, one can calculate the electron spontaneous emission radiative lifetime of intersubband transitions between any two initial and final states:

$$\tau_{if}^{\text{rad}} = \frac{6\pi\epsilon_0 c^3 \hbar^2}{e^2 n} \frac{m^*}{(\hbar v_{if})^2 S_{if}}. \quad (5)$$

Here n is the refractive index set to 3.3, ϵ_0 is the vacuum permittivity, c is the speed of light, and e is the elementary charge [37]. Then the radiative power spectrum can be calculated summing over all subbands in the PQW:

$$P(\hbar\omega) = \sum_{i>f}^N \frac{\rho_i \hbar v_{if} \Gamma}{\pi \tau_{if}^{\text{rad}} (\hbar\omega - \hbar v_{if})^2 + \Gamma^2}. \quad (6)$$

Here ρ_i is the carrier density in each subband, Γ is the spectral broadening set to 0.5 meV for a better line resolution instead of typical 5 meV [37]. The spectra are calculated with the constant carrier density in the subbands.

3. Results and discussion

3.1. PQW design for THz emission

With only variable parameter being l_w , the best solutions for 2.5 and 7 THz PQWs are shown in Fig. 1(a, b), respectively. The first design contains 24 equidistant energy subbands separated by 10.34 meV within the 146 nm width PQW. The second design has 9 equidistant energy subbands separated by 28.95 meV within the 52.2 nm width PQW. THz emission is realized through the intersubband carrier transitions successively from the upper down to the lowest subbands. Selection rules defined by the probability govern electron intersubband transitions and allowed transitions are between every 1st, 3rd, 5th, etc. neighbour subbands. However, the transitions between adjacent subbands have the greatest probability as compared to other ones. A relatively wide PQW if compared to rectangular QWs is in part responsible for greater stability over the applied external electric field and temperature.

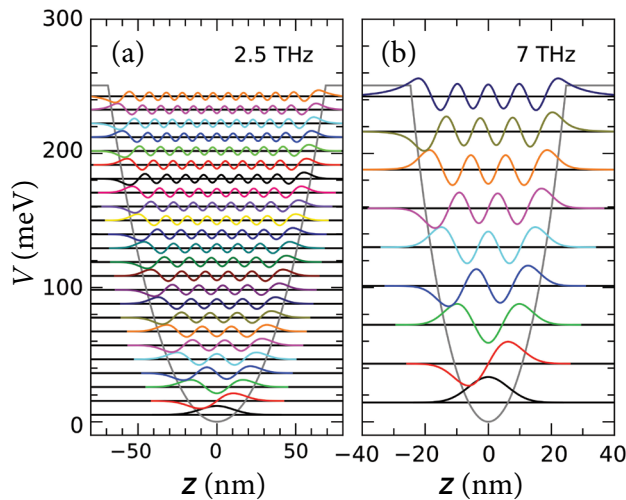


Fig. 1. PQW in the conduction band of GaAs/ $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ structure for 2.5 THz (a) and 7 THz (b) emission. The width of PQW defines the energy separation between subbands. The 146 nm width PQW results in 10.34 meV subband separation and 24 equidistant energy subbands in the well. The 52.2 nm width PQW results in 28.95 meV subband separation and 9 equidistant energy subbands in the PQW.

In Fig. 2, the distance between subbands is depicted as a function of potential energy of the well. Better results were achieved with the quartic term

added to the square one, as declared in Eq. (1). It effectively takes into account the influence of higher order electron effective mass change from GaAs to $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$. As a consequence, the modelled PQW width becomes narrower and it is 138.08 and 49.4 nm for 2.5 and 7 THz designs, respectively. Even though the quartic term improved the arrangement of subbands in PQWs, the energy distance of the uppermost subbands decreases due to the finite barrier height, as seen in Fig. 2. This calculation result has a significant influence on the radiative power spectra that will be discussed latter.

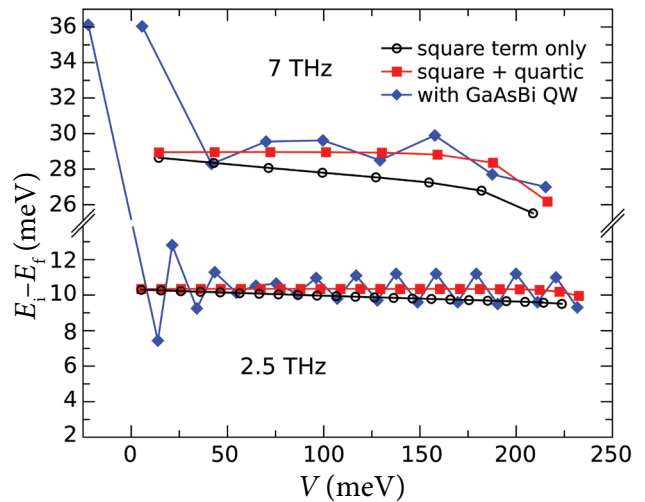


Fig. 2. Energy separation between the initial subband E_i and adjacent final subband E_f dependence on E_f in the PQW potential V for 2.5 and 7 THz design emitters. The open black dots show the energy separation calculated taking into account only the square term and solid red (online) squares show square and quartic terms in Eq. (1). The blue (online) diamonds show the energy separation for GaAs/AlGaAs PQW with 7 nm GaAsBi/GaAs QW in the centre.

3.2. Radiative lifetime

One may expect that a greater number of subbands leads to higher power of radiation due to the overall number of electron transitions that contribute to the increase of single band emission. However, it is not true because radiative lifetime increases with a greater PQW width. It is the result of radiative lifetime being inversely proportional to the energy separation in the power of three and to the dipole matrix element in the power of two, as seen in Eqs. (4) and (5). It gives a non-trivial dependence of the radiative lifetime of intersubband transition on the frequency set by the design.

To study this issue in more detail we modelled a number of PQWs with different well widths from 8.5 nm with only 2 subbands to 146 nm with 24 subbands in the well. The results are plotted in Fig. 3, where the calculated radiative lifetime is depicted as a function of PQW width together with the subband separation energy and oscillator strength of the 2 lowermost subbands of PQWs. One can see that the relaxation time of radiative intersubband transition is increasing quadratically with a well width from 76 ns for the narrowest PQW up to $1.69 \mu\text{s}$ for 52.2 nm (7 THz design) PQW and $13.16 \mu\text{s}$ for 146 nm (2.5 THz design) PQW. The increase of lifetime is largely governed by the energy difference decrease. The oscillator strength also decreases with the increasing PQW width with the same dependence as the one for energy difference between the subbands versus PQW width. It means that intersubband transitions in the THz range are significantly weaker than in the infrared spectral range. Another interesting result (not shown here) is that the radiative lifetime is shorter for the transitions between upper subbands and extends for the transitions towards lower adjacent subbands.

3.3. Depopulation and efficiency of spontaneous intersubband transition

With the calculated lifetime one can roughly estimate the efficiency of THz emission with respect to other carrier scattering processes that take place in the quantum system. Various scattering processes have to be taken into account to evaluate the THz emission efficiency. In Fig. 4(a), a schematic representation of carrier excitation and relaxation processes is depicted. First of all, the carriers are (1) photoexcited with the laser radiation selectively from the uppermost valance to the uppermost conduction band PQW subbands. In the PQW with $h\nu_{\text{if}} < \hbar\omega_{\text{LO}}$, where $\hbar\omega_{\text{LO}}$ is LO phonon energy equal to 36 meV for GaAs, electrons can relax in one of the following scattering mechanisms: (2) spontaneous radiative intersubband transition to lower subbands of PQW emitting photons in the THz range, (3) non-radiative longitudinal acoustic (LA) phonon scattering, (4) electron scattering due to interface roughness, (5) non-radiative electron–electron scattering, and (6) spontaneous radiative interband transition.

The lifetime calculation with a simultaneous consideration of scattering processes is a quantum

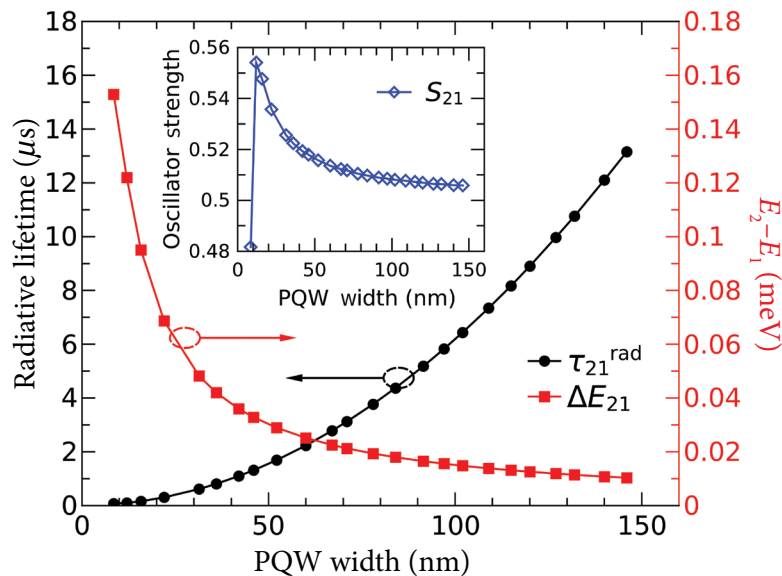


Fig. 3. Radiative lifetime τ_{21}^{rad} (black dots), equidistant energy difference between two lowermost subbands ΔE_{21} (red (online) squares) as a function of PQW width which defines the equidistant energy and emission frequency of THz emitter. The inset shows the oscillator strength S_{21} (blue (online) diamonds) dependence on the PQW width.

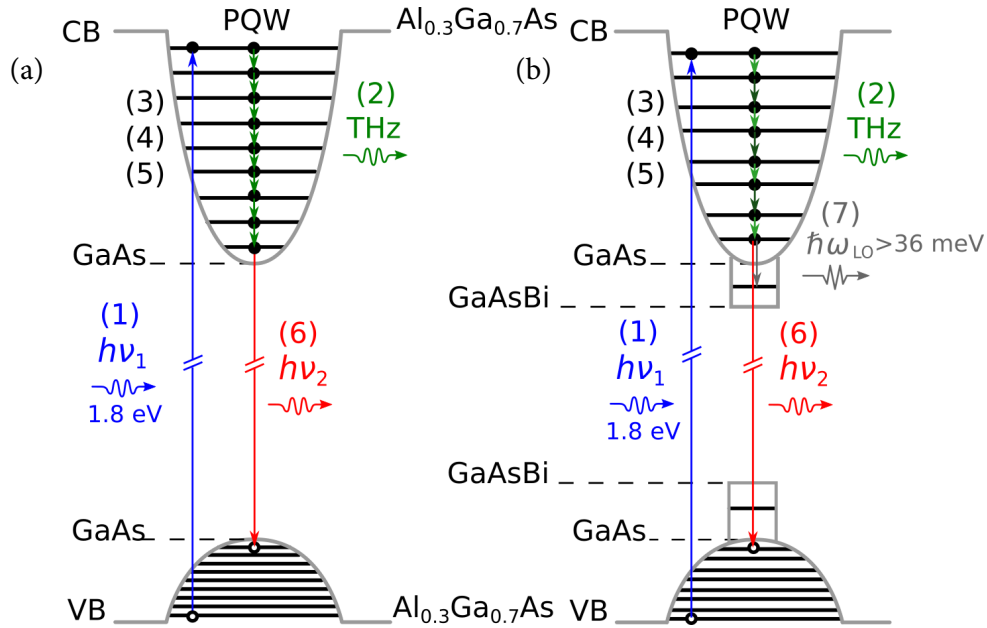


Fig. 4. Schematic diagram of the processes involved in carrier dynamics in the active area of PQW THz emitter without (a) and with (b) additional rectangular potential at the bottom of PQW: (1) absorption of excitation photon, (2) spontaneous radiative intersubband transition giving rise to THz radiation, (3) non-radiative acoustic phonon scattering, (4) electron scattering due to interface roughness, (5) non-radiative electron–electron scattering, (6) spontaneous radiative interband transition and (7) non-radiative optical phonon scattering.

mechanical problem which converges into solving the rate equations derived from the Fermi's golden rule for a particular quantum system. A number of theoretical studies addressing this problem have been carried out for GaAs/AlGaAs quantum structures owing to the fact that this material system is well-studied for practical applications, i.e. semiconductor lasers, QW infrared photodiodes, quantum cascade lasers, etc. In this work, for rough estimate we use the results available through the theoretical work by others [42, 43, 35, 44].

One can assume that there is enough excitation power density of laser radiation to reach the condition that the highest subbands of conduction band PQW be populated. Then five scattering processes that have the main contribution to carrier relaxation with characteristic lifetimes are taken into account. The relaxation time for LA phonon scattering is 250 ps and electron scattering by interface roughness is 2 ns [43]. The non-radiative electron–electron scattering time constant is of 10 ps range [44]. For the radiative interband recombination the theoretical value of 20 ns may be used [42].

The quantum efficiency of the intersubband emission is given by the balance between the radiative and non-radiative relaxation processes and is calculated using

$$\eta = \frac{R_r}{R_r + R_{nr}}, \quad (7)$$

where $R_r = 1/\tau_{if}^{rad}$ is the intersubband transition rate for THz emission, and R_{nr} is the sum of all other processes that compete with the intersubband radiative one and reduce the efficiency of THz emission,

$$R_{nr} = \sum_j^N \frac{1}{\tau_j}, \quad (8)$$

where N is the number of competing scattering processes with 4 abovementioned time constants. The efficiency of THz emission in the PQW drops down with the increase of τ_{if}^{rad} except for saturation to the limit of 1 at extremely fast transit times of less than 0.1 ps. Note that we have obtained the lowest time constant of 76 ns for the narrowest PQW of 8.5 nm in width yielding quantum efficiency 1.26×10^{-4} . In the case of designed PQWs

for 7 and 2.5 THz the efficiency is 5.66×10^{-6} and 7.27×10^{-7} , respectively, with the above defined scattering times. The calculated efficiency value is two orders of magnitude greater than the reported experimental PQW device value 4.4×10^{-8} [24].

Now, if we compare the scattering times, it becomes obvious that under the condition $\hbar v_{\text{if}} < \hbar \omega_{\text{LO}}$ the fastest scattering process is the electron–electron interaction with a typical time constant of 10 ps range and the other ones remain much slower. However, to depopulate the lowest subbands of PQW to effectively remove the carriers, i.e. faster than from the upper subbands, one can introduce the LO scattering process with the typical time constant 0.2 ps [43]. Note that it is around 4 orders of magnitude shorter than that of the interface roughness scattering and 5 orders of magnitude shorter than the interband recombination. For comparison, the electron dephasing relaxation time in the subband is 0.14 ps [45]. With significantly shorter LO phonon scattering time the second subband of PQW is depopulated faster than the higher subbands. To widen the energy separation between the second and the first subbands, a rectangular GaAsBi/GaAs QW may be formed in the centre of PQW, as shown in Fig. 4(b). In this new band arrangement the carriers from the upper subbands transit down to one adjacent subband with the highest probability and emit the THz photons. The electrons that reach the second subband are scattered with the LO phonons much faster than electrons from other subbands leaving the vacancy for other ones. It opens the possibility to depopulate the bottom of PQW and to overcome the carrier crowding effect which eventually stalls the THz generation due to the fact that $\tau_{\text{if}}^{\text{rad}}$ is greater for the transitions between lower subbands.

The subband arrangement changes with the rectangular potential added to the bottom of PQW. The simulations revealed that the optimal subband arrangement with the smallest deviation from the targeted subband separation (10.34 and 28.95 meV) is achieved with 7 nm well width and 1.7 and 0.45% Bi content in the GaAsBi/GaAs QW for 2.5 and 7 THz designs, respectively. The energy separation between rearranged subbands is shown in Fig. 2. Now the energy separation between

the first and the second subband is increased to 36 meV and the energy separation between other subbands is deviated not more than the impact of quartic term to the parabolic dependence of potential energy on distance in Eq. (1). On the one hand, it can be tolerated for a broadband PQW based THz source. On the other hand, the subbands rearrangement has a significance to the dipole matrix element d_{if} , the oscillator strength S_{if} and the intersubband radiative lifetime $\tau_{\text{if}}^{\text{rad}}$.

The efficiency of the intersubband radiative process between the two lowermost subbands in PQW with the depopulation by LO phonon scattering is calculated using Eqs. (7) and (8). Now the number of competing scattering processes is 5 with the same time constants for each (see Fig. 4 and the attribution in the text). The LO phonon scattering reduces the efficiency by nearly 2 orders of magnitude and it is 1.16×10^{-7} and 1.49×10^{-8} for 7 and 2.5 THz emitters, respectively. Therefore the carriers are effectively depopulated from the 2nd subband and these conditions may be favourable for electrons from higher PQW subbands to occupy the vacancies in lower energy states leading to enhancement in THz emission through the increase of intersubband radiative transition probability in the quantum system.

3.4. Emission spectra

Knowing the spontaneous radiative transition time $\tau_{\text{if}}^{\text{rad}}$ of every electron transition over all PQW subbands, one can calculate the emitted power spectrum of the given quantum system using Eq. (6). The radiative power spectra of PQWs are shown in Fig. 5. First, spectra for 2.5 and 7 THz emission PQWs are calculated without an additional rectangular potential at the bottom of PQW. The emission spectrum of 2.5 THz design shows the main spectral line at 2.48 THz with two visible satellite lines at 7.5 and 12.5 THz frequency, i.e. 5 THz apart from each other. These are intersubband radiation maximums corresponding to the 3rd and 5th neighbour subbands with non-zero dipole matrix elements d_{if} . The design for 7 THz has the main emission line split with the maximum at 7 THz and a weaker line at 6.36 THz which is caused by transition between the uppermost subbands (see Figs. 1, 2). The satellite emission line due to electron transition to

the 3rd neighbour subband is observed at 20.84 and 20.17 THz. Numerically significant non-zero d_{if} elements for transitions to the 5th neighbour subbands in the case of 7 THz design are situated already beyond the spectral range of interest at 35 THz frequency and therefore that is not shown in Fig. 5.

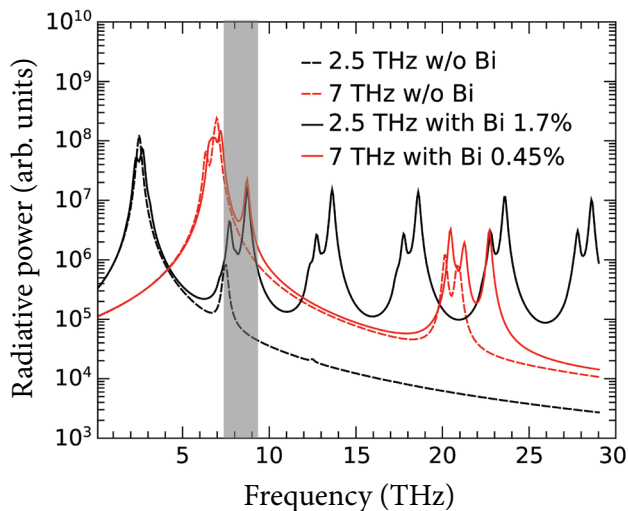


Fig. 5. Radiative power spectra of 2.5 and 7 THz PQWs (dashed lines) and PQWs with GaAsBi/GaAs single QW at the centre (solid lines) for downshift of the first subband 36 meV below the 2nd subband to enable LO scattering of electrons. The gray area indicates the spectral interval for the *reststrahlen* region of GaAs.

The creation of additional potential with GaAsBi/GaAs QW in the centre of PQW changes the subbands energy arrangement and also the oscillator strength S_{if} of intersubband transitions. As a result, the main radiative power spectra of PQWs are slightly wider due to the deviation from the equienergetic arrangement of subbands, but the intensity remains unchanged. Note that we have not taken into account the distribution of carriers over the subbands assuming it constant. It may change the intensity of spectral lines; however the intensity of satellite spectral lines changes dramatically due to a greater oscillation strength between the subbands because of the rearrangement. For the 2.5 THz source design a significant increase is visible for electron transitions to every 3rd, 5th, 7th and 9th neighbour subbands resulting in emission lines with peak intensity at 8.7, 13.6, 18.6, 23.6 and 28.5 THz, respectively. The same

holds for the 7 THz emitter. Note that the spectral lines that fall in the gray area are forbidden to travel in the structure due to the *reststrahlen* region of GaAs [32]. The intensity of satellite lines is also increased and a fine structure appears due to the deviation from the equidistant energy subbands arrangement. It can be beneficial for incoherent broad-band or multi-band THz emitters.

The modelled nanostructures of GaAsBi/GaAs QW in GaAs/AlGaAs PQW can be realized using the molecular beam epitaxy technique for THz torch device fabrication. The THz torch device is proposed as an optically excited *pin* diode with the applied external electric field for carrier control in the PQW active region. The recent advance in the growth of GaAsBi epilayers and nanostructures [46, 47, 31] makes bismide an attractive option for THz emitters employing intersubband transitions instead of interband carrier recombination. The calculations show a significant influence of subband rearrangement to the radiation power spectra of THz torch due to the addition of rectangular GaAsBi/GaAs potential to AlGaAs/GaAs PQW for the carrier depopulation mechanism. More exact performance of the THz torch device can be modelled by solving the rate equations and calculating scattering time constants for the given quantum system as those are parameters sensitive to subband arrangement. The distribution of carriers over the PQW states also has a noticeable influence on emission spectra and efficiency. The built-in electric field needs to be taken into account in order to obtain a more complete description of the system performance. The working THz torch should be designed as a specific *pin* diode with reasonably doped layers for control of carrier density in the active area with quantum wells.

4. Conclusions

Incoherent THz emitting devices based on GaAs/AlGaAs PQW with a central GaAsBi rectangular QW region are modelled for 2.5 and 7 THz emission with a fast depopulation mechanism of the second to the first subband due to the carrier scattering with LO phonons. The energy separation between two lowermost subbands is widened by introducing an additional rectangular potential which is created by GaAsBi/GaAs QW at the centre of PQW. The introduced 7 nm wide GaAsBi QW

with 1.7 and 0.45% Bi content for 2.5 and 7 THz emitters, respectively, increases the energy separation by more than 36 meV to meet the LO phonon energy of GaAs maintaining at the same time the reasonably equidistant arrangement of upper subbands. The calculated radiative power spectra predict the broadening of spectral lines due to the rearrangement of subbands and the enhancement of satellite spectral lines as a result of the greater oscillation strength of transitions between rearranged subbands. Two designs are proposed for fabrication of a novel incoherent THz source, THz torch, with the introduced depopulation of carriers within PQW. It opens the possibility to enhance the THz emission through the increase of probability of intersubband radiative transitions in the proposed solid-state based quantum system.

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**DEPOPULIACIJOS MECHANIZMAS NEKOHERENTINIAM TERAHERCŲ
ŠALTINIUI – THz ŽIBINTUI, PAGRĮSTAM GaAsBi/GaAs KVANTINE DUOBE
PARABOLINĖJE GaAs/AlGaAs KVANTINĖJE DUOBĖJE**

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Santrauka

Parabolinės kvantinės duobės (PKD) yra žinomos kaip tinkama priemonė kompaktiškiems terahercų (THz) šaltiniams. PKD turi vienodais energiniais tarpais pasiskirsčiusias pajuostas, kurios gali būti išdėstytos taip, kad būtų atskirtos kelių meV energiniu atstumu, – tai atitinka THz dažnių ruožą. THz spinduliuotės iš PKD našumui ir galiai padidinti siūlomas naujas būdas išnaudojant žemiausių PKD pajuosčių depopuliaciją. Darbe pateikiama nekoherentinio THz žibinto kaip prietaiso teorinė analizė. Rezultatai rodo, kad siauresnės

draustinių energijų juostos GaAsBi / GaAs stačiakampės duobės įterpimas į GaAs / AlGaAs PKD gali pakeisti pajuosčių išsidėstymą taip, kad būtų įjungiamas greitesnis depopuliacijos mechanizmas, paremtas LO fononų sklaida. Suskaičiuoti spindulinės galios spektrai atskleidžia osciliatoriaus stiprio padidėjimą tarp dėl pridėto GaAsBi stačiakampio potencialo persiskirsčiusių PKD pajuosčių. Išlaugusi tarppajuostinio spindulinio šuolio tikimybė gali tapti našaus, kompaktiško, nekoherentinio THz šaltinio – THz žibinto – veikimo pagrindu.