SATURATED ELECTRON DRIFT VELOCITY AT HIGH ELECTRIC FIELDS IN AlGaAs/GaAs/AlGaAs HETEROSTRUCTURES

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The experimental field dependences of electron drift velocity in the $Al_{0.3}Ga_{0.7}As/GaAs$ quantum well (QW) have no negative slope region and saturate at electric fields in the range of 5–10 kV/cm. The saturated drift velocity in the narrow (10 nm) QW is lower and in the wide (30 nm) QW is larger than the saturated drift velocity in bulk GaAs. The enhancement of the saturated drift velocity is explained by the decrease in the equivalent intervalley and polar optical phonon scattering rates of electrons in upper valleys of a GaAs conduction band with the increase of a QW width. The calculation of these electron scattering rates shows that in AlGaAs/GaAs QW with a width larger than 10 nm, the total confined electron–phonon scattering rate is lower compared with the electron–phonon scattering rate in bulk GaAs. Correspondingly, the electron drift velocity in AlGaAs/GaAs QW is larger than in bulk GaAs at electric fields higher than 10 kV/cm.

Keywords: electron drift velocity, electron-phonon scattering, AlGaAs/GaAs heterostructures

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1. Introduction

The saturation of electron drift velocity at high electric fields in basic semiconductors (Si, GaAs, InGaAs, and others) limits the enhancement of the main parameters of field effect transistors: the maximum cutoff frequency and gain. It has been experimentally observed that the electron drift velocity in GaAs is saturated at $v_{\rm sat} \approx 1 \cdot 10^7$ cm/s at fields exceeding 10 kV/cm [1, 2]. The highest (peak) electron drift velocity value $v_{\rm peak} = 2 \cdot 10^7$ cm/s is achieved at the threshold electric field $F_{\rm peak} \approx 3 \cdot 10^3$ V/cm, when hot electron transfer from lower Γ valley to higher L valleys takes place [3, 4]. In the region of electric fields F = 3-8 kV/cm, the drift velocity–field characteristic, $v_{\rm dr}(F)$, has a negative differential slope, and a differential conductivity is negative ($\sigma_{\rm d} < 0$) due to this transfer.

The electron motion and drift velocity in a twodimensional (2D) electron gas at high electric fields is quite different from that for electrons in bulk samples. The high-field transport in low-dimensional structures is considered in [5–14]. The experimentally measured field dependences of electron drift velocity in HEMT channels show the absence of the region with $\sigma_d < 0$ [15–20].

Recently, it has been experimentally observed that the drift velocity in the GaAs QW at high electric fields $(F \approx 10 \text{ kV/cm})$ exceeds the saturated drift velocity in bulk material [19–23]. We assume that this phenomenon is a result of the decrease of the electron– optical phonon scattering rate (SR) in the QW as compared with the SR in a bulk semiconductor [16, 17].

In this paper, we are looking for conditions at which the saturated electron drift velocity in the GaAs QW can be larger than that in bulk GaAs at high electric fields of $F \approx 10 \text{ kV/cm}$. We have estimated the intervalley and polar optical (PO) phonon SRs of electrons in the GaAs QW with different thicknesses at high electric fields in comparison with the SRs in bulk GaAs and carried out experimental testing of high-field electron drift velocity in the Al_{0.3}Ga_{0.7}As/GaAs structures of different QWs.

2. Equivalent intervalley and PO phonon scattering rates of electrons in the GaAs QW and bulk GaAs at high electric fields

At high electric fields in the range of 8–12 kV/cm, the most part of electrons in GaAs are transferred from Γ valley to upper valleys of a conduction band [3, 4]. Therefore, we suppose that at the high electric fields, the electron drift velocity in GaAs is determined by the SR of electrons in upper L valleys.

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Let us compare the L-valley electron–phonon SR in the GaAs QW at high electric fields with the SR in bulk GaAs. For simplicity, we will consider the intrasubband electron–phonon scattering only in the lowest QW subband.

The frequency of transition of an electron with the initial wave vector \boldsymbol{k} and the energy E to the final state $(\boldsymbol{k'}, E')$ by emission (absorption) of PO phonon with the energy $\hbar\omega_0$ will usually be expressed (see, for example, [24]) as

$$S_{\rm s}(\boldsymbol{k}, \boldsymbol{k'}) = \frac{2\pi}{\hbar} V_{\rm s}(q) G(\boldsymbol{k}, \boldsymbol{k'}) \,\delta(E' - E \pm \hbar\omega_0)$$
$$\times \left(N_q + \frac{1}{2} \pm \frac{1}{2}\right), \tag{1}$$

where \hbar is the Planck's constant, $\delta(E' - E \pm \hbar\omega_0)$ is the Dirac delta function, $N_q = [\exp(\hbar\omega_0/kT) - 1]^{-1}$ is the phonon occupation number, signs '+' and '-' refer to phonon emission and absorption, respectively. The overlap factor $G(\mathbf{k}, \mathbf{k'})$ over the normalization volume V is equal to

$$G(\boldsymbol{k}, \boldsymbol{k'}) = \left| \int_{V} \varphi_{\rm ei} \, \varphi_{\rm ef} \, \varphi_{q} \, \mathrm{d}V \right|^{2}, \qquad (2)$$

where $\varphi_{\rm ei}$, $\varphi_{\rm ef}$ are the normalized electron wave functions in the initial and final states, respectively, φ_q is the phonon wave function. We will use $\varphi_{\rm ez} = \sqrt{2/L_z} \sin \pi z/L_z$ as the z component of the electron wave function in a rectangular QW and the Fang– Howard function $\varphi_{\rm T} = \sqrt{b^3/2} z \exp(-bz/2)$ with $b = 3/z_0$, where z_0 is the average width of the lowest subband inversion layer in a triangular QW.

The matrix element $V_{PO}(q)$ of the electron–PO phonon scattering is taken as

$$V_{\rm PO}(q) = \frac{e^2}{4\pi\varepsilon_0 q^2} \frac{\hbar\omega_0}{2} \left(\frac{1}{\chi_\infty} - \frac{1}{\chi_0}\right),\qquad(3)$$

where e is the electron charge, q = k - k' is the emitted (absorbed) phonon momentum, ε_0 is the permittivity of vacuum, $\chi_{\infty} = 10.9$ and $\chi_0 = 12.3$ are the high and low frequency dielectric constants, respectively, and PO phonon energy is $\hbar\omega_0 = 0.036$ eV in GaAs. The matrix element $V_s(q)$ of the intervalley scattering between equivalent L valleys can be expressed as

$$V_{\rm int}(q) = \frac{D_{\rm LL}^2 \hbar^2}{2\rho \hbar \omega_{\rm LL}} \left(N_{\rm e} - 1 \right),\tag{4}$$

where in the case of GaAs the deformation potential for the scattering between equivalent L valleys is $D_{LL} = 10^9 \text{ eV/cm}$, the material density is $\rho_0 = 5.3 \text{ g/cm}^3$, the intervalley phonon energy is $\hbar\omega_{\rm LL} = 0.029$ eV, the number of L valleys is $N_{\rm e} = 4$.

The scattering rate of an electron with momentum k is equal to

$$W_{\rm s}(\boldsymbol{k}) = \sum_{\boldsymbol{k'}} S_{\rm s}(\boldsymbol{k}, \boldsymbol{k'}) \,. \tag{5}$$

The mean value of the L-valley electron SR with a momentum loss can be estimated as

$$\overline{W_{\rm s}} = \frac{\int W_{\rm s}(E) F_T g(E) f_T(E) \,\mathrm{d}E}{\int g(E) f_T(E) \,\mathrm{d}E} \,, \qquad (6)$$

where $F_T = [1 - f_T(E')]/[1 - f_T(E)]$, g(E) is the electron density of states, and $f_T(E) = \{\exp[(E - E_F)/k_BT_e]+1\}^{-1}$ is the symmetric part of the electron distribution function. We propose that temperature of hot electrons in L valleys at 10 kV/cm can be estimated taking into account the mean electron energy value of $k_BT_e = 0.05$ eV. This value is in agreement with the mean electron energy in L valleys at 10 kV/cm [3, 4].

The electron mobility limited by the intervalley and PO phonon scattering processes at the high fields can be expressed as

$$\mu = \frac{e}{m_{\rm L}} \frac{1}{\overline{W}_{\rm PO} + \overline{W}_{\rm int}} \,. \tag{7}$$

Then the ratio of the mean SR in the QW, $\overline{W}_{QW} = \overline{W}_{POQW} + \overline{W}_{intQW}$, to that in bulk, $\overline{W}_{bulk} = \overline{W}_{PObulk} + \overline{W}_{intbulk}$, coincides with the ratio of the drift velocity in bulk, v_{drbulk} , to that in the QW, v_{drQW} :

$$\frac{W_{\text{bulk}}}{\overline{W}_{\text{OW}}} = \frac{v_{\text{dr}\,\text{QW}}}{v_{\text{dr}\,\text{bulk}}}\,.$$
(8)

Figure 1 demonstrates the dependences of the calculated intrasubband SR (Eq. (6)) in a rectangular QW, \overline{W}_{QW} , on the QW width L_z . One can see that for $L_z >$ 7 nm, \overline{W}_{QW} becomes less than that in bulk material \overline{W}_{bulk} . This means that the electron drift velocity in the GaAs QW in the field range F = 8-12 kV/cm exceeds the drift velocity in bulk material for $L_z >$ 7 nm. For $L_z \approx 20-30$ nm, the electron drift velocity is 2–3 times larger than the drift velocity in bulk material.

However, it is worth to note that with the increase of the QW width L_z , the energy gaps between the electron subbands decrease. In GaAs QW of width $L_z >$ 30 nm, the energy gap between lower subbands became less than 25 meV. Therefore, in the QW wider than 30 nm, additional intrasubband as well as intersubband electron transfer in higher QW subbands manifests itself, and the electron–optical phonon SR is increased.



Fig. 1. Calculated dependences of the mean intrasubband scattering rate of L-valley electrons in a rectangular GaAs QW, \overline{W}_{QW} , on the QW width L_z (full curve) in comparison with the L-valley electron scattering rate in bulk GaAs, \overline{W}_{bulk} (broken curve). Curves with indices 'Int' and 'PO' show contributions of intervalley and PO phonon scattering to the 'Total' scattering rate (\overline{W}_{QW}).

Therefore, at $L_z \rightarrow \infty$, the electron–optical phonon SR in the QW becomes near to that in bulk material.

The calculation of the L-valley electron mean SR in a triangular QW depending on the average width z_0 of the lowest subband inversion layer shows that, at $z_0 >$ 3 nm, $\overline{W}_{\rm QW}$ is less than $\overline{W}_{\rm bulk}$. Therefore, the highfield drift velocity in a triangular QW exceeds that in bulk. In the case of $z_0 = 15$ nm, the drift velocity in the QW is four times larger than the drift velocity in bulk.

Therefore, the simple model of electron–optical phonon SR in a QW predicts that the intervalley and PO phonon SRs of electrons in a moderately wide GaAs QW at high electric fields (8-12 kV/cm) can be significantly less than those in bulk GaAs.

At higher electric fields (F > 12 kV/cm), electrons in GaAs are transferred from L valleys to X valleys [3, 4]. The estimation of the mean SR (Eq. (6)) of X-valley electrons taking into account the equivalent intervalley and PO phonon scattering is shown in Fig. 2. The following parameters are used in calculations: the deformation potential for scattering between



Fig. 2. Calculated dependences of the mean intrasubband scattering rate of X-valley electrons in a rectangular GaAs QW, \overline{W}_{QW} , on the QW width L_z (full curve) in comparison with the X-valley electron scattering rate in bulk GaAs, \overline{W}_{bulk} (broken curve). Other notations are as in Fig. 1.

X valleys, $D_{XX} = 10^9 \text{ eV/cm}$, the effective electron mass, $m_X = 0.41$, the number of X valleys, $N_e = 3$, and $k_BT_e = 0.05 \text{ eV}$, because at the electric field of 10–30 kV/cm, the X-valley electron mean energy corresponds to $k_BT_e = 0.05 \text{ eV}$ [3, 4]. One can see that the X-valley electron–optical phonon SR in the QW at $L_z > 5 \text{ nm}$ is less than the SR in bulk GaAs. At $L_z =$ 15 nm, the X-valley electron drift velocity in the QW exceeds that in bulk by 2 times.

The X-valley electron SR (Fig. 2) is higher than that for L-valley electrons (Fig. 1). Therefore, due to the electron L–X transfer at electric fields F > 12 kV/cm, the current saturation and even negative differential conductivity can take place.

3. Electron drift velocity in the AlGaAs/GaAs/AlGaAs QW at high electric fields

The experimental measurements of the electron drift velocity at high electric fields in the $Al_{0.3}Ga_{0.7}As/GaAs/Al_{0.3}Ga_{0.7}As$ structures for different widths L_z of the GaAs QW were performed. Table 1 shows the parameters of the investigated structures.

AlGaAs/GaAs/AlGaAs sample type	GaAs QW width L_z , nm	Sheet electron concentration $n_{\rm s}$, cm ⁻²
A B* C T**	30 30 10 6***	$\begin{array}{c} 8.4 \cdot 10^{11} \\ 5.9 \cdot 10^{11} \\ 1.25 \cdot 10^{12} \\ 2.6 \cdot 10^{12} \end{array}$

Table 1. The main parameters of the experimentally investigated samples.

* with InAs barriers in the GaAs QW

** the single heterojunction Al_{0.3}Ga_{0.7}As/GaAs modulation-doped structure (triangular QW)

*** width of the lowest subband inversion layer



Fig. 3. Field dependences of the electron drift velocity $v_{\rm dr}$ in the channel of modulation-doped single heterojunction Al_{0.3}Ga_{0.7}As/GaAs structure (triangular QW, T-type sample) with different spacing *d* between the contacts.



Fig. 4. Field dependences of the electron drift velocity $v_{\rm dr}$ in the double-barrier Al_{0.3}Ga_{0.7}As/GaAs/Al_{0.3}Ga_{0.7}As structure with a different width of the GaAs QW: 30 nm in samples *A* and *B* and 10 nm in sample *C*. The spacing between the contacts is $d = 10 \,\mu$ m. Sample *B* has three thin (1 ML InAs) phonon barriers inserted into the GaAs layer. The full curve represents the field dependence of the drift velocity in bulk GaAs [1].

All samples have $100 \times 100 \ \mu m^2$ ohmic contacts (Au/Ni/Ge) with different spacing d between them (from 10 to 100 μ m).

Figures 3 and 4 show the field dependences of electron drift velocity in modulation-doped Al_{0.3}Ga_{0.7}As/GaAs structures with different QW widths. One can see that the field dependence $v_{\rm dr}(F)$ in the QW is sublinear and have no region with the negative slope where $\sigma_{\rm d} < 0$. It is worth to note that the threshold field for velocity saturation decreases about 3 times with increasing the QW width in a range of 10–30 nm (Fig. 4). These drift velocity field dependences are obtained from the experimental current–voltage characteristics I(V) using the measured low-field sheet electron concentration $n_{\rm s}$.

Figure 3 demonstrates the $v_{\rm dr}(F)$ in the QW of the single heterojunction T-type structures (see Table 1). One can see that, at F = 10 kV/cm, the electron drift velocity exceeds the maximum saturated drift velocity in bulk GaAs by a factor of 1.5. This is in agreement with the predicted increase in drift velocity in a triangular QW. The triangular QW approximation gives the calculated ratio of $W_{\text{bulk}}/W_{\text{QW}} = 1.8$ for $z_0 = 6 \text{ nm}$ at $n_{\text{s}} = 2.6 \cdot 10^{12} \text{ cm}^{-2}$.

Figure 4 shows field dependences of the electron drift velocity in the double barrier $Al_{0.3}Ga_{0.7}As/GaAs/Al_{0.3}Ga_{0.7}As$ structures (*A*-, *B*-, and *C*-type samples).

In sample *C* with the narrow QW of width $L_z = 10$ nm, the drift velocity at electric fields of F > 6 kV/cm saturates and does not exceed the velocity in bulk GaAs. This is in agreement with the SR estimation for a narrow QW (see Fig. 1). The velocity saturation takes place at $F \ge 5$ kV/cm.

In samples A and B with a wider QW ($L_z = 30$ nm), the predicted increase of the drift velocity over that in bulk material is observed. Velocity saturation takes place at F > 12 kV/cm. In sample A at F =15 kV/cm, the drift velocity exceeds the saturated drift velocity in bulk by a factor of 1.6.

The largest increase of the drift velocity is observed experimentally in sample *B*. This structure contains three thin (1 monolayer of InAs) PO phonon barriers dividing the GaAs well into four narrow phonon wells. In papers [16, 17] it has been shown that the separation of the QW by thin InAs phonon walls and localization of the confined PO phonons in narrow phonon wells significantly decrease the electron-phonon SR. At F = 15 kV/cm, the drift velocity in sample *B* achieves 2.1·10⁷ cm/s.

Therefore, the experimental data confirm the predicted increase of the electron drift velocity in a moderately wide GaAs QW over the maximum saturated drift velocity in bulk GaAs.

It is worth to note that similar experimental measurements of the drift velocity at high electric fields F > 10 kV/cm were performed in Refs. [19] and [20]. These investigations have confirmed the increase of the drift velocity in the QW larger than 10 nm as compared to the saturated drift velocity in bulk GaAs.

4. Conclusions

We therefore conclude that the enhancement of the electron drift velocity at high electric fields (>10 kV/cm) in a wide (L > 10 nm) Al_{0.3}Ga_{0.7}As/ GaAs QW over the maximum saturated electron drift velocity in bulk material takes place. For the enhancement of the drift velocity in the QW, the decrease in the equivalent intervalley and polar optical phonon scattering rates of electrons in upper valleys of the GaAs conduction band with increasing the QW width is responsible.

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SOTIES ELEKTRONŲ DREIFO GREITIS STIPRIUOSE ELEKTRINIUOSE LAUKUOSE ĮVAIRIALYČIUOSE AIGaAs/GaAs/AIGaAs DARINIUOSE

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Santrauka

Eksperimentiškai tirtos elektronų dreifo greičio priklausomybės nuo elektrinio lauko stiprio $Al_{0,3}Ga_{0,7}As/GaAs$ kvantinėse duobėse. Parodyta, kad šios priklausomybės neturi neigiamo polinkio srities laukuose nuo 5 iki 10 kV/cm. Soties dreifo greitis siaurose kvantinėse duobėse (10 nm) yra mažesnis, o platesnėse (30 nm) – didesnis už soties dreifo greitį tūriniame GaAs. Soties dreifo greičio padidėjimas yra aiškinamas elektronų, esančių aukštesniuose GaAs laidumo juostos X ir L slėniuose, sklaidos tarpjuostiniais ir poliniais optiniais fononais silpnėjimu, kai kvantinės duobės plotis didėja. Atlikti šių sklaidų spartų skaičiavimai parodė, kad suminė elektronų sklaidos optiniais fononais sparta platesnėse už 10 nm AlGaAs/GaAs kvantinėse duobėse yra mažesnė negu elektronų sklaidos optiniais fononais sparta tūriniame GaAs. Atitinkamai, elektronų dreifo greitis AlGaAs/GaAs kvantinėse duobėse yra didesnis negu šis greitis tūriniame GaAs stipresniuose negu 10 kV/cm elektriniuose laukuose.